

## DAfStb Heft 617: Attachment 3-1 to Part 3:

### Notation and Formulary for the ACI-DAfStb Shear Databases vuct-PC-DS and vuct-PC-DK for p.c. beams without stirrups subjected to point loads

#### Database vuct-PC-DS

##### notation of test

No.	running number
Author	Reference: author, year
Test Specimen	specimen as named by author
Units	dual input in Imperial units or SI-units in vuct-PC-DS; Imp. units are converted into SI-units; all calculations in SI-units

##### section properties

b	b	[in → mm]	width of flange
bw	b <sub>w</sub>	[in → mm]	width of web
h	h	[in → mm]	height of beam
hf	h <sub>f</sub>	[in → mm]	height of flange
hh,top	h <sub>h,top</sub>	[in → mm]	height of top haunch
hw	h <sub>w</sub>	[in → mm]	height of web
hft	h <sub>ft</sub>	[in → mm]	height of tension flange
hhbot	h <sub>h,bot</sub>	[in → mm]	height of bottom haunch
bft	b <sub>ft</sub>	[in → mm]	width of tension flange
Ac	A <sub>c</sub>	[mm <sup>2</sup> ]	gross area of concrete section
z <sub>c2</sub>	z <sub>c2</sub>	[mm]	distance of CGS from top fibre

loading and geometry

aa	$a_A$	[in → mm]	dimension of support plate in direction of beam axis
af	$a_F$	[in → mm]	dimension of loading plate in direction of beam axis
ba	$b_A$	[in → mm]	distance between support axis and beam end
L	L	[in → mm]	span
c_	c	[in → mm]	distance between point loads
a	a	[in → mm]	distance of point load F from support axis
kap	$\kappa = \frac{a}{d}$	[ - ]	moment-shear-force ratio
cc	$c_c$	[in → mm]	minimum concrete cover

longitudinal tension reinforcement

ds	$d_s$	[in → mm]	effective depth of reinforcement
bars_t	nr. + type of bars	[ - ]	number and type of bars (text description)
ns	$n_s$	[ - ]	number of bars
dst	$\varnothing_{st}$	[in → mm]	average diameter
fr	$f_r$	[ - ]	r = ribbed bars; 0 = plain bars; blank = not reported
As	$A_s$	[in <sup>2</sup> → mm <sup>2</sup> ]	area of reinforcing steel for long. reinf.
alphaas	$\alpha_{as}$	[ - ]	coefficient for anchorage (hook 0.7; straight 1.0; anchorage plate 0.01)
rhos	$\rho_s = \frac{A_s}{b \cdot d} \cdot 100$	[ % ]	geometrical percentage of long. reinforcement
rhosw	$\rho_{sw} = \frac{A_s}{b_w \cdot d} \cdot 100$	[ % ]	geom. perc. of long. reinforcement related to $b_w$
fsy	$f_{sy}$	[ksi → MPa]	yield strength of steel

esy	$\varepsilon_{sy} = \frac{f_{sy}}{E_s}$	[‰]	steel strain at yield ( $E_s = 200.000 \text{ MPa}$ )
ft	$f_t$	[ksi → MPa]	tensile strength (measured or nominal)
beta_fs	$\beta_{fs} = f_t / f_{sy}$	[ - ]	ratio
euk	$\varepsilon_{uk}$	[ % ]	steel strain at maximum steel stress

longitudinal compression reinforcement

bars_c	nr. + type of bars	[ - ]	number and type of bars (text description)
d_s2	$d_{s2}$	[in → mm]	distance of compress. reinforc. from compress. edge
n_s2	$n_{s2}$	[ - ]	number of bars
d_st2	$\varnothing_{st2}$	[in → mm]	average diameter of compr. bars
A_s2	$A_{s2}$	[in <sup>2</sup> → mm <sup>2</sup> ]	area of compr. bars
f_sy2	$f_{sy2}$	[ksi → MPa]	yield strength of compression bars

prestressing steel

dpbot	$d_{pbot}$	[in → mm]	effective depth of prestressing steel at bottom
dpweb	$d_{pweb}$	[in → mm]	effective depth of prestressing steel in web
dptop	$d_{ptop}$	[in → mm]	effective depth of prestressing steel at top
type	type	[ - ]	number and type of prestressing
btype	bond type	[ - ]	bond type for anchorage check, 1 = strand
p_method	pre / post	[ - ]	pre- or posttensioning
diaps	$\varnothing_{ps}$	[in → mm]	nominal diameter
frp	$f_{rp}$	[ - ]	r = ribbed, 0 = plain
Apbot	$A_{pbot}$	[in <sup>2</sup> → mm <sup>2</sup> ]	area of bottom prestressing steel
Apweb	$A_{pweb}$	[in <sup>2</sup> → mm <sup>2</sup> ]	area of web prestressing steel

$A_{ptop}$	$A_{ptop}$	$[in^2 \rightarrow mm^2]$	area of top prestressing steel
$A_p$	$A_p = A_{pbot} + A_{pweb} + A_{ptop}$	$[mm^2]$	area of prestressing steel
$\alpha_{ap}$	$\alpha_{ap}$	$[-]$	coefficient for anchorage (straight 1.0; anchorage plate 0.01)
$\rho_p$	$\rho_p = \frac{A_{pbot}}{b \cdot d} \cdot 100$	$[\%]$	geom. reinf. ratio of prestr. steel
$\rho_{pw}$	$\rho_{pw} = \frac{A_{pbot}}{b_w \cdot d} \cdot 100$	$[\%]$	geom. reinf. ratio of prestr. steel related to $b_w$
$\rho_l$	$\rho_l = \rho_s + \rho_p$	$[\%]$	geom. reinf. ratio
$\rho_{lw}$	$\rho_{lw} = \rho_{sw} + \rho_{pw}$	$[\%]$	geom. reinf. ratio
$E_p$	$E_p$	$[MPa]$	young's modulus of prestressed steel (if not given $E_p = 200.000 \text{ MPa}$ )
$f_{py}$	$f_{py}$	$[ksi \rightarrow MPa]$	yield strength = $f_{p0,1k}$
$\epsilon_{py}$	$\epsilon_{py} = f_{py} / E_p \cdot 1000$	$[\%]$	steel strain at yield
$f_p$	$f_p$	$[ksi \rightarrow MPa]$	tensile strength (measured or nominal)
$\beta_{fp}$	$\beta_{fp} = f_p / f_{py}$	$[-]$	ratio
$\epsilon_{puk}$	$\epsilon_{puk}$	$[\%]$	steel strain at maximum steel stress
$\lambda$	$\lambda = \frac{A_{pbot} f_{py}}{(A_{pbot} f_{py}) + (A_s \cdot f_{sy})}$	$[-]$	prestressing ratio
$d$	$d = \frac{(A_{pbot} f_{py} \cdot d_{pbot}) + (A_s \cdot f_{sy} \cdot d_s)}{(A_{pbot} f_{py}) + (A_s \cdot f_{sy})}$	$[mm]$	average effective depth of tension chord
<u>prestress</u>			
$P_{bot\_rep}$	$P_{bot,rep}$	$[kip \rightarrow kN]$	reported prestressing force of bottom tendons
$P_{web\_rep}$	$P_{web,rep}$	$[kip \rightarrow kN]$	reported prestressing force of web tendons
$P_{top\_rep}$	$P_{top,rep}$	$[kip \rightarrow kN]$	reported prestressing force of top tendons

$P_{rep}$		$P_{rep}$	[kN]	prestressed force as reported
$P_{eff}$		$P_{eff}$	[kN]	effective prestress force at test including all losses
$P_{check}$	$P_{rep} = P_{eff}$ :	$P_{check} = 1$	[ - ]	check if reported prestressing force is = $P_{eff}$
$\delta_{sigp}$	$P_{check} = 1$ :	$\Delta\sigma_p = 0$	[MPa]	assumption of loss of prestress
	$P_{check} = 0$ :	$\Delta\sigma_p = 200$	[MPa]	
$P_{bot}$		$P_{bot}$	[kN]	prestressing force of bottom tendons
$P_{web}$		$P_{web}$	[kN]	prestressing force of web tendons
$P_{top}$		$P_{top}$	[kN]	prestressing force of top tendons
$z_{pbot}$		$z_{pbot}$	[mm]	distance of bottom tendons from CGS
$z_{pweb}$		$z_{pweb}$	[mm]	distance of web tendons from CGS
$z_{ptop}$		$z_{ptop}$	[mm]	distance of top tendons from CGS
$P$		$P = P_{bot} + P_{web} + P_{top}$	[kN]	total prestressing force
$\sigma_{cp}$		$\sigma_{cp} = P/A_c$	[MPa]	axial concrete stress at CGS
$\nu_{cp}$		$\nu_{cp} = \sigma_{cp}/f_{lc}$	[ - ]	non-dimensional prestressing force
$M_p$		$M_p = z_{pbot} \cdot P_{bot} + z_{pweb} \cdot P_{web} + z_{ptop} \cdot P_{top}$	[kNm]	moment due to prestress
$\sigma_{pp}$		$\sigma_{pp} = P/A_p$	[MPa]	steel stress due to prestress
$V_p$		$V_p$	[kip → kN]	vertical component of effective prestressing force (only relevant in –dt and –cb databases)
<u>axial force</u>				
$N$		$N$	[kN]	axial force
$\sigma_{cN}$		$\sigma_{cN} = N/A_c$	[MPa]	axial concrete stress at CGS
$\nu_{cN}$		$\nu_{cN} = \sigma_{cN}/f_{lc}$	[ - ]	non-dimensional axial force

nu_c	$v_c = \sigma_c / f_{1c}$	[ - ]	ratio for total axial force stress with $\sigma_c = \sigma_{cp} + \sigma_{cN}$
<u>concrete compressive strength</u>			
diaa	$\varnothing_a$	[in → mm]	max. diameter of aggregates
fccyl	$f_{c,cyl}$	[ksi → MPa]	cylinder strength of concrete
dimcyl		[in → mm]	dimension of cylinders
f1ccyl	$f_{1c,cyl}$	[MPa]	uniaxial compr. strength derived from $f_{c,cyl}$
fccu	$f_{c,cube}$	[ksi → MPa]	cube strength of concrete
dimcu		[in → mm]	dimension of cubes
f1ccu	$f_{1c,cu}$	[MPa]	uniaxial compr. strength derived from $f_{c,cube}$
fcpr	$f_{c,prism}$	[ksi → MPa]	prism strength of concrete
dimpr		[in → mm]	dimension of prisms
f1cpr	$f_{1c,pr}$	[MPa]	uniaxial compr. strength derived from $f_{c,prism}$
f1c	$f_{1c}$	[MPa]	uniaxial compr. strength of concrete
cs_method	CS test method	[ - ]	testing method (cyl; cu; pr)
<u>concrete tensile strength</u>			
fctfl	$f_{ct,fl}$	[ksi → MPa]	modulus of rupture
dimfl		[in → mm]	dimension of control specimen
f1ctfl	$f_{1ct,fl}$	[MPa]	axial tensile strength derived from $f_{ct,fl}$
fctsp	$f_{ct,sp}$	[ksi → MPa]	splitting tensile strength
dimsp		[in → mm]	dimension of control specimen
f1ctsp	$f_{1ct,sp}$	[MPa]	axial tensile strength derived from $f_{ct,sp}$
f1cttest	$f_{1ct,test}$	[MPa]	test value for axial tensile strength
ts_method	TS test method	[ - ]	testing method (fl; sp)
betacttest	$\beta_{ct,test} = f_{1ct,test} / f_{1c}$	[ - ]	ratio

$f_{lctm,cal}$	$f_{lctm,cal}$	[MPa]	calculated value of axial tensile strength
$\beta_{ct,cal}$	$\beta_{ct,cal} = f_{lctm,cal} / f_{lc}$	[ - ]	ratio
<u>mechanical reinforcement ratios</u>			
$\omega_s$	$\omega_s = \frac{A_s \cdot f_{sy}}{b \cdot d \cdot f_{lc}}$	[ - ]	mech. reinf. ratio of reinf. steel in tension chord
$\omega_p$	$\omega_p = \frac{A_{pbot} \cdot f_{py}}{b \cdot d \cdot f_{lc}}$	[ - ]	mech. reinf. ratio of prestr. steel in tension chord
$\omega_l$	$\omega_l = \omega_s + \omega_p$	[ - ]	mech. reinf. ratio of tension chord
<u>test</u>			
$g$	$g = A_c \cdot 24$	[kip/in→kip/ft →kN/m]	self-weight
$V_g$	$V_g = g \cdot (0,5 \cdot c + (a - x_r))$	[kip → kN]	shear force due to self-weight
$F$	$F$	[kip → kN]	failure load
$V_{u,F+g,Rep}$	$V_{u,F+g,Rep}$	[kip → kN]	shear force at failure without self-weight
$V_{u,Rep}$	$V_{u,Rep}$	[kip → kN]	shear force at failure with self-weight (from report)
$V_{u,g+F}$	$V_{u,g+F}$	[kip → kN]	shear force at failure with self-weight
$\beta_r$	$\beta_r$	[ ° ]	measured crack angle
$x_{r,meas}$	$x_{r,meas}$	[in → mm]	measured distance of failure crack from support axis
$x_r$	$x_r$	[in → mm]	calculated dist. of failure crack from support axis
tof		[ - ]	type of failure as reported
oft		[ - ]	other failure type
com		[ - ]	comment

check

contr [ - ] =0 if data is not controllable based on report

konx =IF(OR(f1c=0;fpy=0;Vu\_Rep=0;Pbot\_rep=0;kap=0;contr=0);0;1)

kon\_61 =IF(d>0;IF(kap>=2,4;1;0);0)

kons1 =konx·kon\_61

kon\_62 =IF(d>0;IF(kap<2,4;1;0);0)

kon\_24 =kon\_62·konx

b\_\_\_bw =IF(b=bw;1;0)

conversion factors

1 inch = 25,4 mm

1 pound = 4,448 N

1 kip = 4,448 kN

1 klbf ft = 1,36 kNm

1 psi = 1/145 MPa

1 ksi = 1000/145 MPa

1 kp = 9,81 N

1 kp/cm<sup>2</sup> = 9,81/100 MPa = 9,81/100 N/mm<sup>2</sup>

type of prestressing

SWS/270 Seven- Wire Strand ( $f_{pk} = 270$  ksi)

SWS/250 Seven- Wire Strand ( $f_{pk} = 250$  ksi)

TFWS Three- and Four- Wire Strand ( $f_{pk} = 250$  ksi)

PW Prestressing Wire

SPB/145 Smooth Prestressing Bars ( $f_{pk} = 145$  ksi)

SPB/160 Smooth Prestressing Bars ( $f_{pk} = 160$  ksi)

DPB Deformed Prestressing Bars

**Database vuct-PC-DK**Internal forces at failure

Mu	$M_u = \frac{V_{u, Re p} \cdot a}{1000}$	[kNm]	max. moment at failure
muu	$\mu_u = \frac{M_u \cdot 10^6}{b \cdot d^2 \cdot f_{lc}}$	[ - ]	non-dimensional value of ultimate moment
vutest	$v_{u, test} = \frac{\tau_{u, test}}{f_{lc}} = \frac{V_{u, Re p}}{b_w \cdot z_{test} \cdot f_{lc}}$	[ - ]	non-dimensional value of ultimate shear force with respect to compressive strength
vutestct	$v_{u, test, ct} = \frac{\tau_{u, test}}{f_{lctm, cal}} = \frac{V_{u, Re p}}{b_w \cdot z_{test} \cdot f_{lctm, cal}}$	[ - ]	non-dimensional value of ultimate shear force with respect to tensile strength

Check of flexural failure

kapc		$\kappa_c = 1 - \frac{f_{lc}}{250}$	[ - ]	coefficient for maximum stress of stress block
epp		$\varepsilon_{pp} = \frac{\sigma_{pp} \cdot 10^3}{E_p}$	[‰]	stress in prestr. steel due to prestress
omgr	$A_s = 0$	$\omega_{gr} = \kappa_c \cdot \frac{0,4 \cdot d_{pbot}}{d}$	[ - ]	limiting reinforcement ratio
	$A_s > 0$	$\omega_{gr} = \kappa_c \cdot \frac{0,4 \cdot d_s}{d}$	[ - ]	

xsi11		$\xi_{11} = \frac{\omega_1}{\kappa_c}$	[ - ]	factor for depth of compression zone
zeta11	$\omega_{gr} > \omega_1$	$\zeta_{11} = 1 - \frac{1}{2} \cdot \frac{\omega_1}{\kappa_c}$	[ - ]	factor for inner lever arm $z_1$
acall	$A_s = 0$	$a_{call} = 1,0$	[ - ]	auxiliary factor
	$A_s > 0$	$a_{call} = \frac{\omega_p}{\varepsilon_{py}} + \frac{\omega_s \cdot d_s}{d_{pbot} \cdot \varepsilon_{sy}}$	[ - ]	
bcall	$A_s = 0$	$b_{call} = \varepsilon_{pp} + 3,5$	[ - ]	auxiliary factor
	$A_s > 0$	$b_{call} = \omega_p \cdot \frac{\varepsilon_{pp} + 3,5}{\varepsilon_{py}} + \omega_s \cdot \frac{3,5}{\varepsilon_{sy}} \cdot \left( 2 \cdot \frac{d_s}{d_{pbot}} - 1 \right)$	[ - ]	
ccall	$A_s = 0$	$c_{call} = \varepsilon_{pp} \cdot 3,5 - \frac{\kappa_c \cdot \varepsilon_{py} \cdot 3,5}{\omega_p}$	[ - ]	auxiliary factor
	$A_s > 0$	$c_{call} = \omega_p \cdot \frac{\varepsilon_{pp} \cdot 3,5}{\varepsilon_{py}} + \omega_s \cdot \frac{3,5^2}{\varepsilon_{sy}} \cdot \left( \frac{d_s}{d_{pbot}} - 1 \right) - \kappa_c \cdot 3,5 \cdot \frac{d_{pbot}}{d}$	[ - ]	
deltaep		$\Delta\varepsilon_p = \frac{-b_{call} + \sqrt{b_{call}^2 - 4 \cdot a_{call} \cdot c_{call}}}{2 \cdot a_{call}}$	[ % ]	strain of prestr. steel
xsi12	$A_s = 0$	$\xi_{12} = \frac{3,5}{3,5 + \Delta\varepsilon_p}$	[ - ]	factor for depth of compression zone
	$A_s > 0$	$\xi_{12} = \frac{d_{pbot}}{d} \cdot \frac{3,5}{3,5 + \Delta\varepsilon_p}$	[ - ]	
zeta12	$\omega_{gr} < \omega_1$	$\zeta_{12} = 1 - \frac{1}{2} \cdot \xi_{12}$	[ - ]	factor for inner lever arm $z_2$
muflex11		$\mu_{u,flex11} = \omega_1 \cdot \zeta_{11}$	[ - ]	non-dimensional moment
muflex12	$A_s = 0$	$\mu_{u,flex12} = \omega_1 \cdot \frac{\Delta\varepsilon_p + \varepsilon_{pp}}{\varepsilon_{py}} \cdot \zeta_{12}$	[ - ]	non-dimensional moment

	$A_s > 0$	$\mu_{u,flex12} = \omega_p \cdot \frac{\Delta \varepsilon_p + \varepsilon_{pp}}{\varepsilon_{py}} \cdot \left( \frac{d_{pbot}}{d} - \frac{1}{2} \cdot \xi_{12} \right) +$ $\frac{\omega_s}{\varepsilon_{sy}} \cdot \left( \frac{d_s}{d_{pbot}} \cdot (\Delta \varepsilon_p + 3,5) - 3,5 \right) \cdot \left( \frac{d_s}{d} - \frac{1}{2} \cdot \xi_{12} \right)$	[ - ]	
muflex1		$\mu_{u,flex1}$	[ - ]	non-dimensional moment at flexural failure
xsi_1	$\zeta_{11} = 0$	$\xi_1 = \xi_{12}$	[ - ]	factor for depth of compression zone
	$\zeta_{11} \neq 0$	$\xi_1 = \xi_{11}$	[ - ]	
x_1		$x_1 = \xi_1 \cdot d$	[mm]	depth of compression zone
Mu_flex1		$M_{u,flex1} = \frac{\mu_{u,flex1} \cdot b \cdot d^2 \cdot f_{lc}}{1000^2}$	[kNm]	moment at flexural failure
beta_flex1		$\beta_{flex1} = \frac{\mu_u}{\mu_{u,flex1}}$	[ - ]	ratio of attained to calc. moment
betax1		$\beta_{x1} = \frac{x_1}{h_f}$	[ - ]	ratio of depth of compression zone to height of flange of beams without haunch
betax2		$\beta_{x2} = \frac{x_1}{h_f + h_{h,top}}$	[ - ]	ratio of depth of compression zone to height of flange of beams with haunch
kon_hfu			[ - ]	=1 if $b > b_w$ and $\beta_{x1} > 1$
hhtop2	$\beta_{x1} > 1$ and $\beta_{x2} < 1$	$h_{h,top2} = x_1 - h_f$	[mm]	height of top haunch in compression
	$\beta_{x1} > 1$ and $\beta_{x2} > 1$	$h_{h,top2} = h_{h,top}$	[mm]	
alpha_fl		$\alpha_{fl}$	[ ° ]	inclination of top haunch
A_cc		$A_{cc}$	[mm <sup>2</sup> ]	area of compression zone in T- and I-beams
z_cc		$z_{cc}$	[mm]	inner lever arm z in T- and I-beams

My_hf	$M_{y,hf}$	[kNm]	moment at failure of longitud. tension reinforcement in T- and I beams	
Mc_fl	$M_{c,fl}$	[kNm]	moment at failure of compression zone in T- and I-beams	
Mfl_min	$M_{fl,min}$	[kNm]	moment at flexural failure (min. of $M_{y,hf}$ , $M_{c,fl}$ )	
Mu_flex	$M_{u,flex}$	[kNm]	moment at flexural failure (min. of $M_{u,flex1}$ , $M_{fl,min}$ )	
betaflex	$\beta_{flex} = \frac{M_u}{M_{u,flex}}$	[ - ]	ratio of attained to calc. moment	
FlexF	comment	[ - ]	remark (FF = flexural failure)	
Vu_flex	$v_{u,flex} = \frac{M_{u,flex}}{a} \cdot 1000$	[kN]	shear force at flexural failure	
xsi	for kon_hfu = 0	$\xi = \xi_1$	[ - ]	factor for depth of compression zone
	for kon_hfu = 1	$\xi = \frac{(h_f + h_{h,top})}{d}$	[ - ]	
x	$x = \xi \cdot d$	[mm]	depth of compression zone	
zeta	$\zeta = 1 - \frac{1}{2} \cdot \xi$	[ - ]	factor for z	
z_	$z = \zeta \cdot d$	[mm]	inner lever arm	
muflex	$\mu_{u,flex} = \frac{M_{u,flex}}{b \cdot d^2 \cdot f_{lc}}$	[ - ]	non-dimensional moment at flexural failure	

Calculation of  $z_{test}$ 

acal	$A_s = 0$	$a_{cal} = 0$	[ - ]	auxiliary value
	$A_s > 0$	$a_{cal} = \frac{\omega_s^2}{\epsilon_{sy}^2} + 1,968 \cdot 0,9578 \cdot \omega_s \cdot \omega_p \cdot \frac{1}{\epsilon_{sy} \cdot \epsilon_{py}} + 0,968 \cdot 0,9578^2 \cdot \frac{\omega_p^2}{\epsilon_{py}^2}$	[ - ]	
bcal	$A_s = 0$	$b_{cal} = 0$	[ - ]	auxiliary value
	$A_s > 0$	$b_{cal} = -2 \cdot \kappa_c \cdot \frac{d_s}{d} \cdot \left( \frac{\omega_s}{\epsilon_{sy}} + \omega_p \cdot 0,9578 \cdot 0,968 \cdot \frac{1}{\epsilon_{py}} \right) + 1,968 \cdot \left( \omega_s \cdot \omega_p \cdot \frac{\epsilon_{pp}}{\epsilon_{sy}} \cdot \epsilon_{py} \right) + 2 \cdot 0,9578 \cdot 0,968 \cdot \omega_p^2 \cdot \frac{\epsilon_{pp}}{\epsilon_{py}^2}$	[ - ]	
ccal	$A_s = 0$	$c_{cal} = 0$	[ - ]	auxiliary value
	$A_s > 0 :$	$c_{cal} = 0,968 \cdot \frac{\omega_p^2}{\epsilon_{py}^2} \cdot \epsilon_{pp}^2 - 2 \cdot 0,968 \cdot \kappa_c \cdot \frac{d_s}{d} \cdot \frac{\omega_p}{\epsilon_{py}} \cdot \epsilon_{pp} + 2 \cdot \kappa_c \cdot \mu_u$	[ - ]	
estest		$\epsilon_{stest} = \frac{-b_{cal} - \sqrt{b_{cal}^2 - 4 \cdot a_{cal} \cdot c_{cal}}}{2 \cdot a_{cal}}$	[‰]	strain in reinf. steel
deltaepstest		$\Delta \epsilon_{ptest} = \epsilon_{stest} \cdot \frac{d_{pbot} - \xi_{test} \cdot d}{d_s - \xi_{test} \cdot d}$	[‰]	strain in prestr. steel
sigp	$A_s = 0$	$\sigma_p = \frac{\kappa_c \cdot f_{py}}{\omega_p} \cdot \left( 1 - \sqrt{1 - 2 \cdot \frac{\mu_u}{\kappa_c}} \right)$	[MPa]	stress in prestr. steel
	$A_s > 0$	$\sigma_p = E_p \cdot (\epsilon_{pp} + \Delta \epsilon_{ptest})$	[MPa]	stress in reinf. steel
xsi_1test	$A_s = 0$	$\xi_{1,test} = \frac{\omega_p \cdot \sigma_p}{\kappa_c \cdot f_{py}}$	[ - ]	factor for depth of compression zone

	$A_s > 0$	$\xi_{1,test} = \frac{\varepsilon_{stest}}{\kappa_c} \cdot \left( \frac{\omega_s}{\varepsilon_{sy}} + \frac{\omega_p}{\varepsilon_{py}} \cdot 0,9578 \right) + \frac{\varepsilon_{pp} \cdot \omega_p}{\kappa_c \cdot \varepsilon_{py}}$	[ - ]	
x_1test		$x_{1,test} = \xi_{1,test} \cdot d$	[mm]	depth of compression zone $x_{1,test}$
zeta1test		$\zeta_{1,test} = 1 - \frac{1}{2} \cdot \xi_{1,test}$	[ - ]	factor for inner lever arm $z_{1,test}$
z_1test		$z_{1,test} = \zeta_{1,test} \cdot d$	[mm]	inner lever arm $z_{1,test}$
betax1test		$\beta_{x1,test} = \frac{x_{1,test}}{h_f}$	[ - ]	ratio of depth of compression zone $x_{test}$ to height of flange of beams without haunch
betax2test		$\beta_{x2,test} = \frac{x_{1,test}}{h_f + h_{h,top}}$	[ - ]	ratio of depth of compression zone $x_{test}$ to height of flange of beams with haunch
kon_hfute			[ - ]	=1 if $b > b_w$ and $\beta_{x1,test} > 1$
hhtop2test	$\beta_{x1,test} > 1$ and $\beta_{x2,test} < 1$	$h_{h,top2,test} = x_{1,test} - h_f$	[mm]	height of top haunch in compression
	$\beta_{x1,test} > 1$ and $\beta_{x2,test} > 1$	$h_{h,top2,test} = h_{h,top}$	[mm]	
A_cctest		$A_{cc,test}$	[mm <sup>2</sup> ]	area of compression zone in T- and I-beams
z_cctest		$z_{cc,test}$	[mm]	inner lever arm z in T- and I-beams
z_test	for FlexF = FF	$z_{test} = z$	[mm]	inner lever arm $z_{test}$
	for $\beta_{x1,test} > 1,0$	$z_{test} = z_{cc,test}$	[mm]	
	no FF and $\beta_{x1,test} \leq 1,0$	$z_{test} = z_{1,test}$	[mm]	
xsitest		$\xi_{test} = 2 \cdot (1 - \zeta_{test})$	[ - ]	factor for depth of compression zone
xtest		$x_{test} = \xi_{test} \cdot d$	[mm]	depth of compression zone $x_{1,test}$
zetatest		$\zeta_{test} = z_{test}/d$	[ - ]	factor for inner lever arm $z_{1,test}$

Check of anchorage

lbprov	for $a_A \neq 0$ ; $b_A \neq 0$	$l_{b,prov} = a_A/2 + b_A - (h - d)$	[mm]	provided anchorage length
	for $a_A = 0$ ; $b_A \neq 0$ :	$l_{b,prov} = b_A$	[mm]	
	for $a_A \neq 0$ ; $b_A = 0$ :	$l_{b,prov} = a_A + 0,1 d$	[mm]	
	for $a_A = b_A = 0$ :	$l_{b,prov} = 0,25 \cdot d$	[mm]	
Fsa	for $a_A \neq 0$	$F_{sa} = V_{u,Rep} \cdot \left[ 0,5 \frac{a_A}{z} + 2,20 \frac{h-d}{z} + 0,873 \right]$	[kN]	steel force to be anchored
	for $a_A = 0$	$F_{sa} = V_{u,Rep} \cdot \left[ 0,5 \frac{0,2 \cdot d}{z} + 2,20 \frac{h-d}{z} + 0,873 \right]$	[kN]	
alpha		$\alpha = \frac{F_{sa}}{A_s \cdot f_{sy}}$	[-]	ratio of force to be anchored and steel force at yield
sslau		$\sigma_{slau} = \frac{F_{sa}}{A_s}$	[MPa]	steel stress near end support
lbreq1	for $\alpha \leq 1$	$l_{breq1} = \alpha_{as} \cdot d_{st} \cdot \sigma_{slau} / (9 \cdot f_{lctm,cal})$	[mm]	required anchorage length
lbreq2	for $\alpha > 1$	$l_{breq2} = \alpha_{as} \cdot d_{st} \cdot f_{sy} / (9 \cdot f_{lctm,cal})$	[mm]	required anchorage length
betalb1		$\beta_{lb1} = \frac{l_{breq1}}{l_{bprov}} \text{ or } \frac{l_{breq2}}{l_{bprov}}$	[ - ]	ratio of required to provided anchorage length
Fsaprov	for $\alpha \leq 1$ and $\beta_{lb1} > 1$	$F_{sa,prov} = \frac{F_{sa}}{\beta_{lb1}}$	[kN]	provided tension force at end support
	for $\alpha \leq 1$ and $\beta_{lb1} \leq 1$	$F_{sa,prov} = F_{sa}$	[kN]	

	for $\alpha > 1$ and $\beta_{lb1} > 1$	$F_{sa,prov} = \frac{A_s \cdot f_{sy}}{\beta_{lb1}}$	[kN]	
	for $\alpha > 1$ and $\beta_{lb1} \leq 1$	$F_{sa,prov} = A_s \cdot f_{sy}$	[kN]	
deltaFsa_p		$\Delta F_{sa,p} = F_{sa} - F_{sa,prov}$	[kN]	force difference
spau		$\sigma_{pau} = \frac{\Delta F_{sa,p}}{A_{pbot}}$	[MPa]	stress in prestr. steel due to $\Delta F_{sa,p}$
konfpy_anch		$kon_{fpy,anch}$	[ - ]	check if prestressing steel yields if $\Delta F_{sa,p}$ is applied
lbreq3	for SWS:	$l_{breq3} = \frac{\alpha_{ap} \cdot diaps}{4 \cdot 0,55 \cdot f_{lctm,cal}} \cdot \left( 0,5 \cdot \frac{P_{bot}}{A_{pbot}} + 0,8 \cdot \sigma_{pau} \right)$	[mm]	required anchorage length (pre-tensioned)
	for others:	$l_{breq3} = \frac{\alpha_{ap} \cdot diaps}{4 \cdot 0,641 \cdot f_{lctm,cal}} \cdot \left( 0,7 \cdot \frac{P_{bot}}{A_{pbot}} + 1,0 \cdot \sigma_{pau} \right)$	[mm]	required anchorage length (pre-tensioned)
lbreq4		$l_{breq4} = \alpha_{ap} \cdot diaps \cdot \left( \frac{P_{bot}}{A_{pbot}} + \sigma_{pau} \right) / (9 \cdot f_{lctm,cal})$	[mm]	required anchorage length (post-tensioned)
betalb		$\beta_{lb} = \frac{l_{breq3}}{l_{bprov}} \text{ or } \frac{l_{breq4}}{l_{bprov}}$	[ - ]	ratio of required to prov. anchorage length
AnchF		comment	[ - ]	AF = anchorage check not fulfilled

criteria for data selection and sorting

kon_1	=IF(flc>12;1;0)
kon_2	=IF(flc<100;1;0)
kon_3	=IF(bw>=50;1;0)
kon_31	=IF(bw>=50;IF(bw<100;1;0);0)
kon_4	=IF(h>=70;1;0)

kon_41	=IF(h=0;IF(ds/0,9>=70;IF(ds/0,9<150;1;0);IF(h>=70;IF(h<150;1;0)));0)
kon_34	=IF(OR(kon_31=1;kon_41=1);0;1)
kon_5	=IF(kap>2,89;1;0)
kon_6	=IF(AND(kap>=2,4;kap<=2,89);1;0)
kon_x7	=IF(oml=0;0;1)
kon_7	=IF(kon_x7=0;0;IF(FlexF="FF";IF(xsi<=0,5;1;0);IF(xsitest<=0,5;1;0))
kon_x8	=IF(betaflex=0;0;1)
kon_8	=IF(kon_x8=0;0;IF(betaflex<1;1;0))
kon_81	=IF(betaflex>=1;IF(betaflex<1,1;1;0);0)
kon_101	=IF(fr="r";1;0)
kon_103	=IF(frp="r";1;0)
kon_10a	=IF(OR(kon_101=1;kon_103=1);1;0)
kon_10b	=IF(AND(kon_10a=0;p_method="Post");1;0)
kon_10	=IF(OR(kon_10a=1;kon_10b=1);1;0)
kon_x11	=IF(betalb=0;0;1)
kon_11	=IF(kon_x11=0;0;IF(betalb<1;1;0))
kon_15	=IF(oft="oft";0;1)
KON_A0a	=kon_1·kon_3·kon_4
KON_A0b	=KON_A0a·kon_7
KON_A0c	=KON_A0b·kon_10
KON_A0	=KON_A0c·kon_15
KON_A21a	=KON_A0·kon_5·kon_8
KON_A22a	=KON_A0·kon_5·kon_81
KON_A2a	=IF(OR(KON_A21a=1;KON_A22a=1);1;0)
KON_A31a	=KON_A0·kon_6·kon_8

KON_A32a	=KON_A0·kon_6·kon_81
KON_A3a	=IF(OR(KON_A31a=1;KON_A32a=1);1;0)
A2a+A3a	=IF(OR(KON_A2a=1;KON_A3a=1);1;0)
KON_A21	=KON_A21a·kon_11
KON_A22	=KON_A22a·kon_11
KON_A2	=IF(OR(KON_A21=1;KON_A22=1);1;0)
KON_A31	=KON_A31a·kon_11
KON_A32	=KON_A32a·kon_11
KON_A3	=IF(OR(KON_A31=1;KON_A32=1);1;0)
A2+A3	=IF(OR(KON_A2=1;KON_A3=1);1;0)
KON_A4a	=KON_A2a·kon_34
KON_A5a	=KON_A3a·kon_34
A4a+A5a	=IF(OR(KON_A4a=1;KON_A5a=1);1;0)
KON_A4	=KON_A2·kon_34
KON_A5	=KON_A3·kon_34
A4+A5	=IF(OR(KON_A4=1;KON_A5=1);1;0)

#### Nominal values of concrete strength

$f_{lck}$	$f_{lck} = f_{lc} - 3,8$	[MPa]	characteristic uniaxial concrete compressive strength
$f_{cm\_cyl}$	$f_{cm\_cyl} = \frac{f_{lc}}{0,95}$	[MPa]	mean cylinder strength of concrete
$f_{ck}$	$f_{ck} = f_{cm\_cyl} - 4$	[MPa]	characteristic cylinder strength
$f'_{c\_prime}$	$f'_c = f_{ck} + 1,6$	[MPa]	specified compressive strength of concrete (ACI, CSA)